## EXAMPLE Problem 4

Linear Expansion A metal bar is 1.60 m long at room temperature, 21°C. The bar is put into an oven and heated to a temperature of 84°C. It is then measured and found to be 1.7 mm longer. What is the coefficient of linear expansion of this material?

# Analyze and Sketch the Problem

- Sketch the bar, which is 1.7 mm longer at 84°C than at 21°C.
- Identify the initial length of the bar,  $L_1$ , and the change in length,  $\Delta L$ .



#### Known:

### **Unknown:**

$$L_1 = 1.60 \text{ m}$$

$$\alpha = ?$$

$$\Delta L = 1.7 \times 10^{-3} \text{ m}$$

$$T_1 = 21^{\circ}\text{C}$$

$$T_2 = 84^{\circ}\text{C}$$

### 2 Solve for the Unknown

Calculate the coefficient of linear expansion using the known length, change in length, and change in temperature.

$$\alpha = \frac{\Delta L}{L_1 \Delta T}$$
=  $\frac{1.7 \times 10^{-3} \text{ m}}{(1.60 \text{ m})(84^{\circ}\text{C} - 21^{\circ}\text{C})}$ 

$$= \frac{1.7 \times 10^{-3} \text{ m}}{(1.60 \text{ m})(84^{\circ}\text{C} - 21^{\circ}\text{C})} \qquad \frac{\text{Substitute } \Delta L = 1.7 \times 10^{-3} \text{ m}, L_{1} = 1.60 \text{ m},}{\Delta T = (T_{2} - T_{1}) = 84^{\circ}\text{C} - 21^{\circ}\text{C}}$$

$$= 1.7 \times 10^{-5} \, ^{\circ}\text{C}^{-1}$$

#### **Math Handbook**

Operations with Significant Digits pages 835-836

### 3 Evaluate the Answer

- Are the units correct? The units are correctly expressed in °C<sup>-1</sup>.
- Is the magnitude realistic? The magnitude of the coefficient is close to the accepted value for copper.

## PRACTICE Problems

Additional Problems, Appendix B

- **39.** A piece of aluminum house siding is 3.66 m long on a cold winter day of -28°C. How much longer is it on a very hot summer day at 39°C?
- **40.** A piece of steel is 11.5 cm long at 22°C. It is heated to 1221°C, close to its melting temperature. How long is it?
- **41.** A 400-mL glass beaker at room temperature is filled to the brim with cold water at 4.4°C. When the water warms up to 30.0°C, how much water will spill from the beaker?
- **42.** A tank truck takes on a load of 45,725 L of gasoline in Houston, where the temperature is 28.0°C. The truck delivers its load in Minneapolis, where the temperature is -12.0°C.
  - a. How many liters of gasoline does the truck deliver?
  - **b.** What happened to the gasoline?
- **43.** A hole with a diameter of 0.85 cm is drilled into a steel plate. At 30.0°C, the hole exactly accommodates an aluminum rod of the same diameter. What is the spacing between the plate and the rod when they are cooled to 0.0°C?
- 44. A steel ruler is marked in millimeters so that the ruler is absolutely correct at 30.0°C. By what percentage would the ruler be incorrect at  $-30.0^{\circ}$ C?

